

4) a) Solution: $x = 2.4$ $y = -0.8$

Possible steps:

Multiply Eq1 by 28, Eq2 by $(x + y)$:

$$\begin{cases} 7(x - y) - 12(y - 2) = 56 \\ x - y = 2(x + y) \end{cases}$$

Remove the brackets, simplify:

$$\begin{cases} 7x - 19y = 32 \\ -x - 3y = 0 \end{cases} \begin{array}{l} + \\ \cdot 7 + \end{array} \rightarrow -40y = 32 \rightarrow y = -0.8$$

$$x \text{ by inserting: } -x - 3y = 0 \rightarrow -x - 3 \cdot (-0.8) = 0 \rightarrow x = 2.4$$

- b) Lösung: The system has infinitely many solutions.
(All the pairs (x,y) that satisfy $-3x + y = 2$ are solutions.)

Remarks:

After eliminating the brackets and simplifying you get two identical equations (or at least multiples of each other):

$$\begin{cases} -3x + y = 2 \\ -3x + y = 2 \end{cases}$$

Hence the solution set of the system equals the solution set of this (doubled) equation.

- c) Two solutions: $x_1 = 1.5$ $y_1 = 0.25$
 $x_2 = -1$ $y_2 = -1$

Possible steps:

$$\text{Solve Eq2 for } y: y = x^2 - 2 \quad (*)$$

Inserting it into Eq1 leads to

$$\frac{x-1}{x^2-2} = 2 \quad | \cdot (x^2-2)$$

Multiply by the denominator term, rearrange, simplify; you get the quadratic equation

$$2x^2 - x - 3 = 0$$

with the above solutions for x .

y -values by inserting into $(*)$.